

# Treating Traffic Asymptotics with Care

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# Main Message

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## Why do we care about traffic asymptotics (limit)?

- use traffic limit as an approximate model for the traffic

However, using the traffic limit as a model **MAYNOT ALWAYS** be appropriate.

- queueing property of the traffic may not be approximated by that of the limit

When we can use the limit as an approximation depends on the nature of our study.

## Why?

- difference between the traffic and its limit may become significant depending on the nature of the study
- queueing: exchange of the limit condition and the queueing functional may not hold

We will illustrate this using two examples.

# Traffic Limit 1: Fractional Brownian Motion (FBM)

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Packet traffic is asymptotically self-similar and long-range dependent.

- Ethernet LAN (*On the Self-Similar Nature of Ethernet Traffic*, Leland et. al, 1994)
- Internet traffic, video traffic

Theoretical justification: superposition of  $n$  on-off processes.

- if we superpose  $n$  on-off processes with heavy-tailed on/off time, then the cumulative packet count process tends toward FBM when  $n \rightarrow \infty$  AND THEN cumulative time scale  $\rightarrow \infty$ . (*Proof of a Fundamental Result in Self-Similar Traffic Modeling*. Taqqu et. al, 1997)
- delicacy of limits: a limit of stable Levy motion when cumulative time scale  $\rightarrow \infty$  AND THEN  $n \rightarrow \infty$

Queueing property of the superposed traffic  $\xrightarrow{n \rightarrow \infty} \not\Rightarrow$  queueing property of a FBM, for a queue of constant service rate, with fixed utilization and a buffer size scales with  $n$ .

- queue size of a FBM input process: Weibullian tail (*Norros, 1994*)
- queue size of the superposed traffic of  $n$  on-off processes as  $n \rightarrow \infty$ : tail behaviour ONLY depends on the on-time distribution  
(*Overflow behavior in queues with many long-tailed inputs*. M. Mandjes and S. Borst, 2000)
  - light-tailed on-time, heavy-tailed off time: exponential tail
  - Pareto on-time: Pareto tail

## Traffic Limit 2: Poisson Arrival with Independent Sizes

Internet packet arrivals tend toward Poisson with independent sizes with increasing statistical multiplexing (superposition). Long-range dependence (LRD) of Internet traffic dissipates with superposition.

- empirical study of 2526 Internet packet header traces (*Cao et al. 2001, 2002*)
- superposition theorem of marked point processes (*Daley and Vere Jones, 1988*)

Internet traffic can not necessarily be substituted by Poisson traffic.

- example: packet count process not independent, fixed correlation function
- why: diminishing LRD component of packet arrivals brings back a non-diminishing dependence of packet counts due to increased packet aggregation

Queueing property of the superposed traffic from  $n$  i.i.d. packet arrival processes

Let  $BEP$  be the buffer exceedance probability. For a queue with constant service rate,

- fixed utilization and buffer size (*Cao and Ramanan 2002*)

$$BEP(\text{superposed traffic}) \xrightarrow{n \rightarrow \infty} BEP(\text{Poisson, independent sizes})$$

- fixed utilization, buffer size scales with  $n$ :

$$BEP(\text{superposed traffic}) \not\xrightarrow{n \rightarrow \infty} BEP(\text{Poisson, independent sizes})$$

(but rather depends on the traffic characteristic of a single source traffic )

(*Botvich+Duffield 95, Courcoubetis+Weber 98, Likhanov+Mazumdar 98, Simonian+Guibert 95, Mandjes+Borst 00*)

# Conclusion

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- be careful when using traffic asymptotic limit as a model
- model the traffic itself rather than using the limit
- check whether the queueing property of the traffic match that of the model